USN

Sixth Semester B.E. Degree Examination, Dec.2015/Jan.2016 Information Theory and Coding

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, selecting atleast TWO questions from each part.

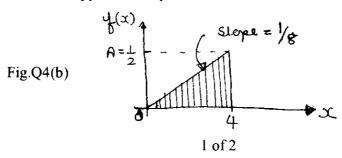
- 2. Standard notations are used.
- 3. Missing data may be suitably assumed.

PART - A

- a. Derive the expression for entropy of a zero memory discrete source and define entropy rate. source efficiency and source redundancy.
 - b. Calculate the entropy rate and entropy of source of a conventional telegraph source with the dash twice as long as a dot and half as probable given: $\int_{\text{dot}} = 0.2 \text{ sec.}$ (10 Marks)
- 2 a. For the Markov source whose state diagram is shown below fig.Q2(a), find the source entropy H and the average information content per symbols in messages containing one, two and three symbols. That is calculating G_1 , G_2 and G_3 . (12 Marks)

Fig.Q2(a)

- b. What are the important properties of codes while encoding a source? Explain with examples. (08 Marks)
- 3 a. Explain with diagram a Binary erasure channel. Derive the expression for channel capacity of a Binary erasure channel.
 - b. Consider a zero memory source alphabet $S = \{S_1, S_2, S_3, S_4, S_5, S_6, S_7\}$ with probabilities $P = \{0.4, 0.2, 0.1, 0.1, 0.1, 0.05, 0.05\}$ construct a Binary Huffman code and compute the code efficiency and redundancy. (10 Marks)
- a. State Shannon Hartley law and derive the expression for channel capacity with infinite 4 Bandwidth.
 - b. A one dimensional variable has a pdf as shown in fig. Q4(b). Determine the entropy of the source producing the variation (ii). If the signal is passed through a linear amplifier of gain of determine the entropy of the output. (10 Marks)



PART - B

- 5 a. What is error control coding? Mention and explain the type of errors occurring in communication channels. (08 Marks)
 - b. For a systematic (7, 4) linear block code the Parity matrix is given by:

$$P = \begin{bmatrix} 111 \\ 110 \\ 101 \\ 011 \end{bmatrix}$$

- i) Find all possible valid code vectors
- ii) Draw the corresponding encoder circuit.
- iii) Draw the syndrome calculation circuit.

(12 Marks)

- 6 a. What is a binary cyclic code? Mention and explain the properties of cyclic codes. (08 Marks)
 - b. For a (7, 4) cyclic code the received vector Z(x) is 1110101 and the generator polynomial is $g(x) = 1 + x + x^3$. Draw the syndrome calculation circuit and correct the single error in the received vector. (12 Marks)
- 7 Write short notes on the following:
 - a. RS codes.
 - b. Shortened cycle code.
 - c. Burst error correcting codes.
 - d. Golay codes.

(20 Marks)

- 8 a. What are the main difference between block codes and convolutional codes? (04 Marks)
 - b. For the convolution encoder the information sequence is d = 10011. Find the output sequence using the following two approaches.
 - i) Time domain approach
- ii) Transform domain approach.

(16 Marks)

